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# A study of stopping power in nuclear reactions at intermediate energies

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*For INDRA Collaboration*

NuSym10 RIKEN, Wako, Japan  
26-28 July.



# Motivations

## Study of transport phenomena in nuclear reactions

- ▶ link with the viscosity (macroscopic degrees of freedom) at low energy ( $E < E_f$ )
- ▶ link with the in-medium nucleon-nucleon cross-section (microscopic dof) at high energy ( $E > E_f$ )

## Be of interest to describe

- ▶ the process of supernova collapse and formation of a neutron star<sup>1</sup>
- ▶ the various mechanisms in nuclear reactions: fusion, deep-inelastic, incomplete fusion<sup>2</sup>

1: J.M. Lattimer and M. Prakash : *Astrophys. J* **550**, 426 (2001).

2: E. Suraud, D. Durand and B. Tamain *Nuclear Dynamics in the Nucleonic Regime*

# INDRA dataset

## Symmetric collisions

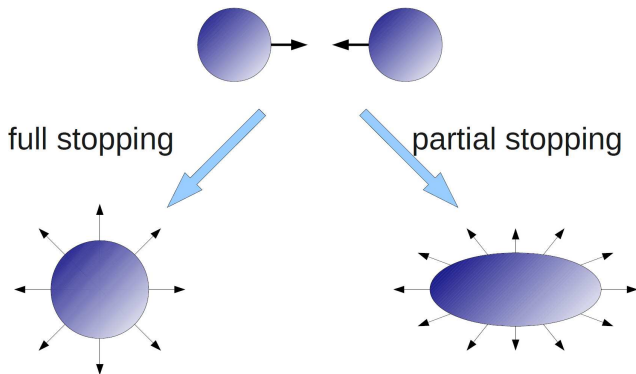
- ▶ Incident energy between 12 and 100 MeV/A
- ▶ Total size between  $A=80$  and  $A=400$

## Isospin pairs at 32 and 45 MeV/A

- ▶  $^{124}\text{Xe} + ^{112}\text{Sn} \Rightarrow N/Z = 1.27$      $\circ \rightarrow \circ$     *PP*
- ▶  $^{124}\text{Xe} + ^{124}\text{Sn} \Rightarrow N/Z = 1.38$      $\circ \rightarrow \circ$     *PN*
- ▶  $^{136}\text{Xe} + ^{112}\text{Sn} \Rightarrow N/Z = 1.38$      $\circ \rightarrow \circ$     *NP*
- ▶  $^{136}\text{Xe} + ^{124}\text{Sn} \Rightarrow N/Z = 1.50$      $\circ \rightarrow \circ$     *NN*
- ▶  *$N/Z$  variation around 15-20%*



## Stopping power measurement



- ▶ memory of entrance channel is lost
- ▶ no preferential axis

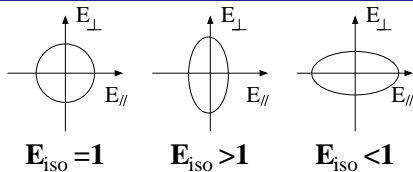
- ▶ memory of the entrance channel is partially conserved
- ▶ preferential direction along the beam axis

## Method

$$E_{iso} = \frac{1}{2} \frac{\sum E_{\perp}}{\sum E_{\parallel}}$$

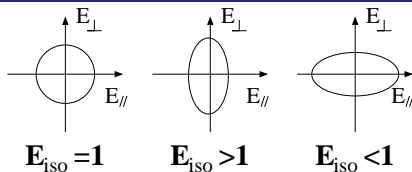
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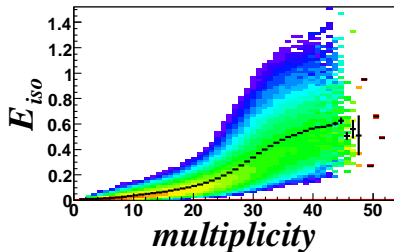


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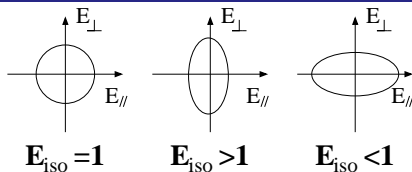


$^{129}\text{Xe} + \text{nat}\text{Sn}$  @ 50 MeV/A



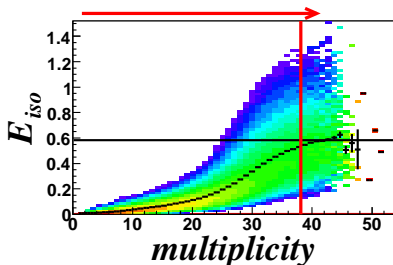
## Method

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$^{129}\text{Xe} + \text{nat}\text{Sn}$  @ 50 MeV/A

*toward central collisions*

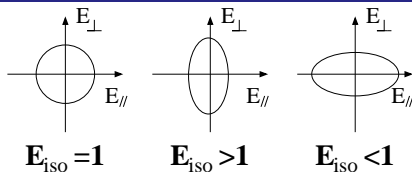


$\Rightarrow$  cross section  $\approx 50\text{mb}$  ( $0.1b_{max}$ )



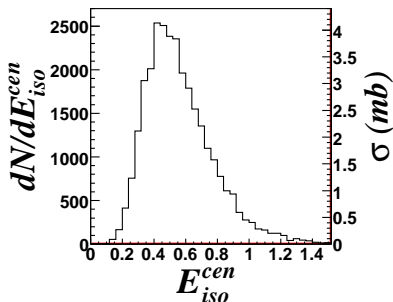
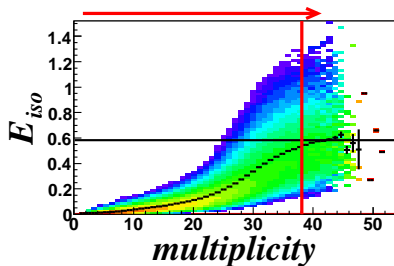
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$^{129}\text{Xe} + ^{\text{nat}}\text{Sn}$  @ 50 MeV/A

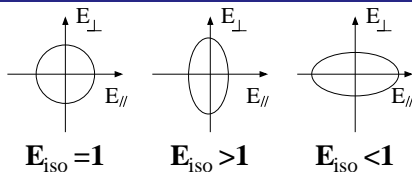
*toward central collisions*



⇒ cross section  $\approx 50\text{mb}$  ( $0.1b_{\text{max}}$ )

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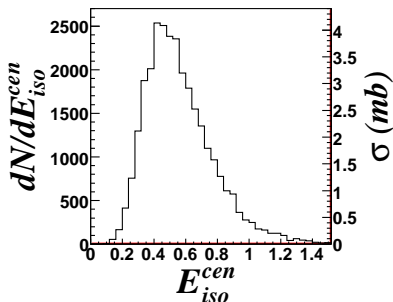
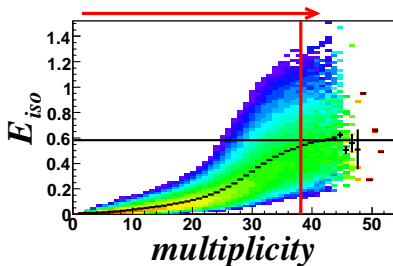


$^{129}\text{Xe} + ^{\text{nat}}\text{Sn}$  @ 50 MeV/A

no full stopping

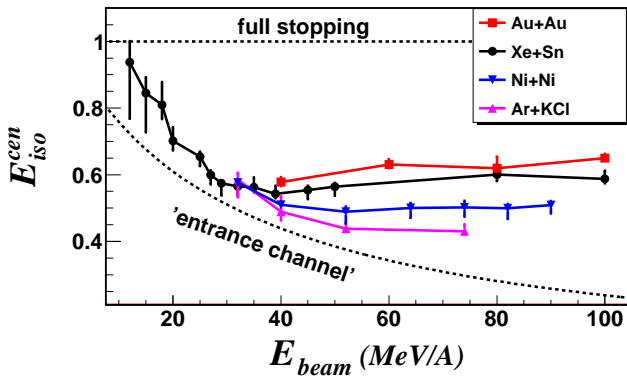
$E_{iso}^{cen} < 1$

*toward central collisions*



$\Rightarrow$  cross section  $\approx 50\text{mb}$  ( $0.1b_{max}$ )

# Systematics

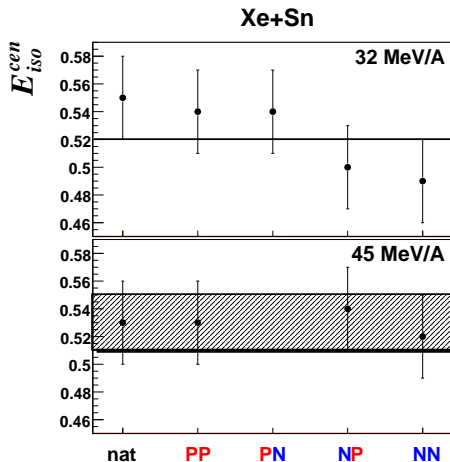


- ▶ minimum at  $E = E_f$
- ▶ saturation above  $E_f$ , and hierarchy with the mass of the system: the higher  $A_{tot}$ , the higher  $E_{iso}$  is
- ▶ transition from one-body to two-body dissipation

## Isospin effect

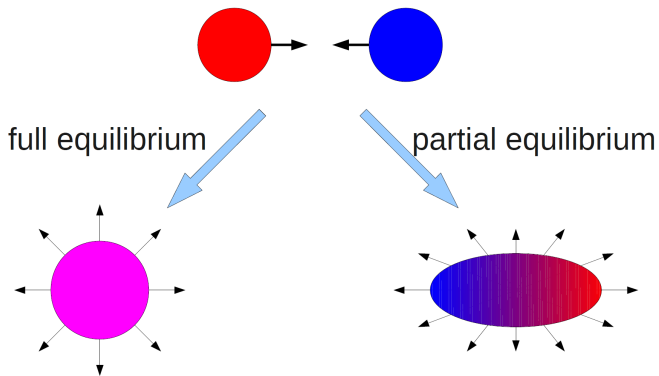
- ▶  $^{129}\text{Xe} + ^{119}\text{Sn} \Rightarrow \text{nat}$
- ▶  $^{124}\text{Xe} + ^{112}\text{Sn} \Rightarrow \text{PP}$
- ▶  $^{124}\text{Xe} + ^{124}\text{Sn} \Rightarrow \text{PN}$
- ▶  $^{136}\text{Xe} + ^{112}\text{Sn} \Rightarrow \text{NP}$
- ▶  $^{136}\text{Xe} + ^{124}\text{Sn} \Rightarrow \text{NN}$

- Error bars are here systematics



- ▶ small effect of the isospin content at  $E$  around  $E_f$  (extension to higher and lower  $E$  are in the perspectives)

## Isospin equilibration



- ▶ memory of entrance channel is lost
- ▶ same isospin everywhere

- ▶ memory of the entrance channel is partially conserved
- ▶ dependence of the isospin along the beam axis

# Isospin diffusion

## Imbalance ratio

$$\tilde{R}_{p/t} = \frac{2R_{p/t} - R_{p/t}^{NN} - R_{p/t}^{PP}}{R_{p/t}^{NN} - R_{p/t}^{PP}}$$

where  $R_{p/t}$  is the normalized yield of different particles in isospin here proton over triton.

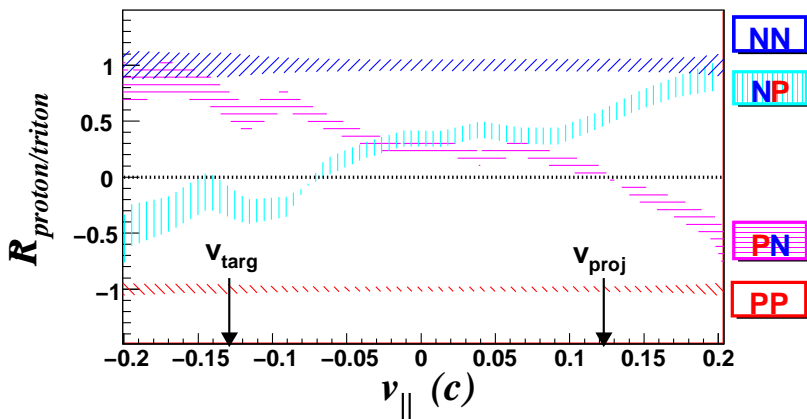
$$\tilde{R}_{proton/triton} = \begin{cases} +1 & \text{if } R_{p/t} = R_{p/t}^{NN} \\ -1 & \text{if } R_{p/t} = R_{p/t}^{PP} \end{cases}$$

F. Rami, PRL **84**, 1120 (2000)

V. Baran, PRC **72**, 064620 (2005)

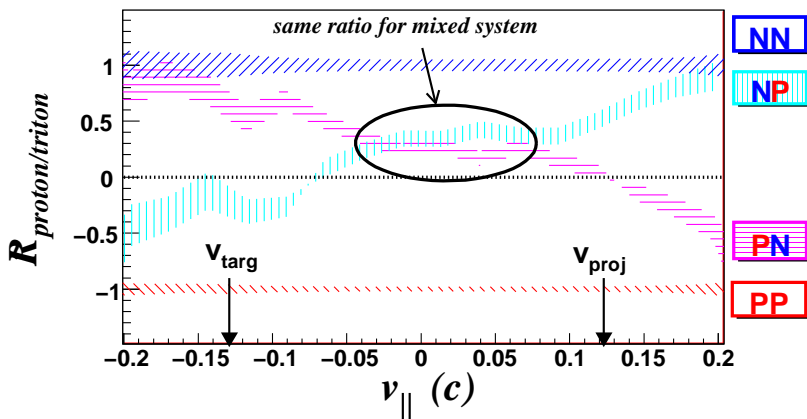
# Proton triton ratio along the beam axis (in central collisions)

Xe+Sn @ 32 MeV/A



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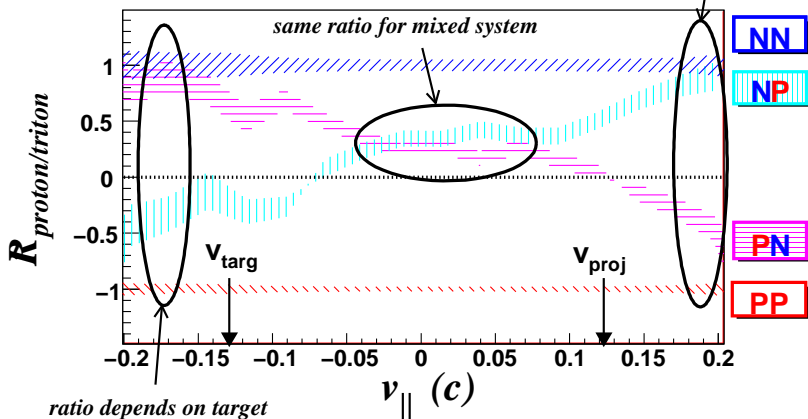




# Proton triton ratio along the beam axis (in central collisions)

Xe+Sn @ 32 MeV/A

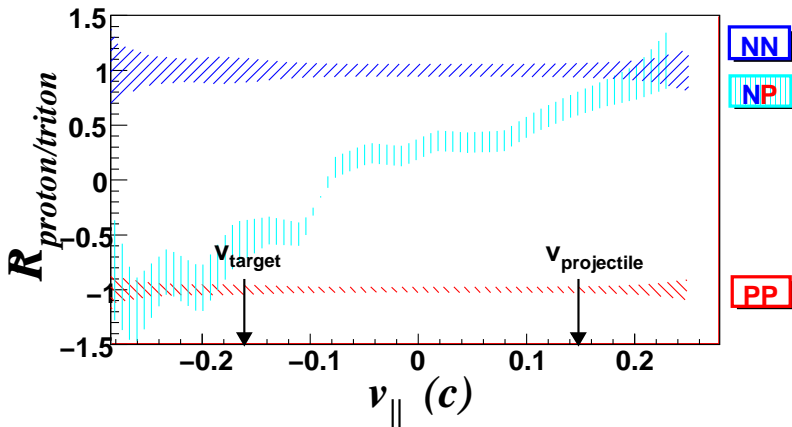
ratio depends on projectile



- ▶ Imbalance ratios shows nuclear transparency at 32A MeV for central collisions

# Proton triton ratio along the beam axis (in central collisions)

Xe+Sn at 45 MeV/A central collisions



- ▶ Imbalance ratios shows nuclear transparency at 45A MeV for central collisions

# Comparison with a microscopic model: ELIE

## Entrance channel

- ▶ geometry + nn collision: mean free path  $\lambda$
- ▶ conservation laws are taken into account :  $\vec{p}$ ,  $E$ ,  $Z$ ,  $N$
- ▶ maximal internal temperature  $T=5.5$  MeV for primary fragments ( $A > 6$ )
- ▶ discrete excited levels are considered up to  $A=10$ , above Fermi gas level density is assumed
- ▶  $N/Z$  memory of the entrance channel : no isospin relaxation
- ▶ nucleons momentum distributions are 2 Fermi spheres at  $T=0$  : sudden approximation (valid at  $E > E_f$ )

## Exit channel

The partition  $\{Z_i, A_i, \vec{r}_i, \vec{p}_i\}$  is propagated in space-time and in-flight statistical secondary decays are considered : SIMON code

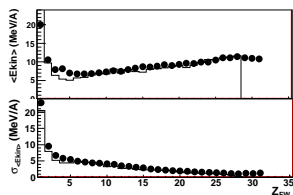
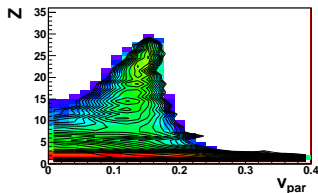
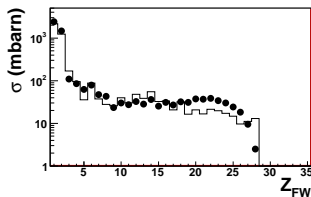
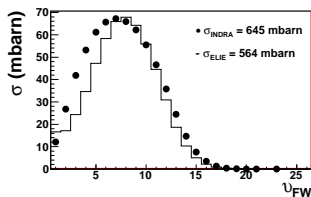
D. Durand, in preparation

# Comparison on some basic observables :

## $Ni + Ni@52A.MeV$

INDRA : selection  $Z_{tot}^{FW} \in [0.8; 1.2]$

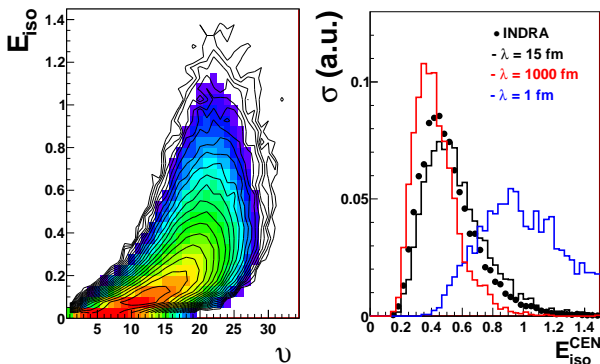
ELIE filtered : selection  $Z_{tot}^{FW} \in [0.8; 1.2]$



- An excellent agreement between ELIE and the INDRA data is found

## Comparison on stopping:

$Ni + Ni@52A.MeV$ , central collisions  $\nu > 26$



- ▶ sensitivity to  $\lambda$  is found for  $E_{iso}^{cen}$ , especially for  $\lambda < (R_{proj} + R_{targ})$
- ▶ data is closer to  $\lambda = 15$  fm ( $> R_{proj} + R_{targ}$ ), suggesting no complete thermalization since the number of collisions per participant is less than 1.

# Summary and Perspectives

## Summary

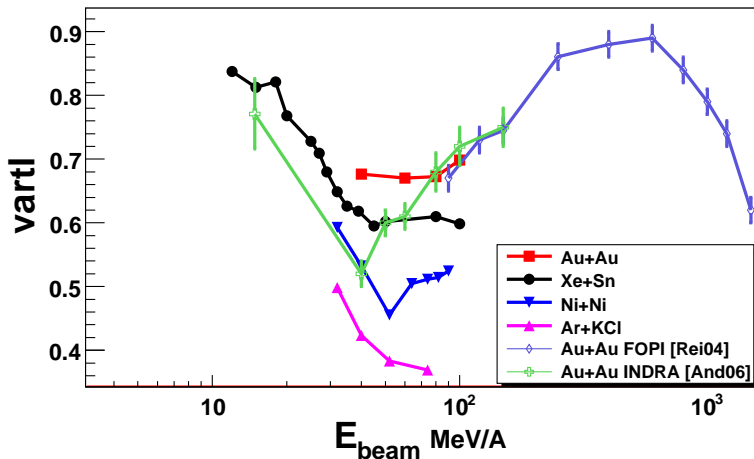
- ▶ Stopping power is minimum around the Fermi energy (30-40 MeV/A)
- ▶ The isospin of the entrance channel has no effect on the stopping around  $E = E_f$ . Is it still true for  $E < E_f$  and  $E \gg E_f$  ?
- ▶ The study of imbalance ratios shows nuclear transparency at 32 and 45A MeV for central collisions

## Perspectives

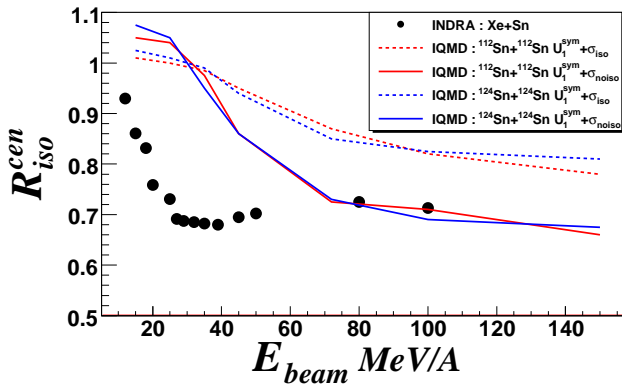
- ▶ Systematic comparison with microscopic models (ELIE, HIPSE, QMD) , ...
- ▶ Study the asymmetric collisions:  $^{181}\text{Ta} + ^{64,68}\text{Zn}$  @ 19, 32, 39A.MeV  
⇒ INDRA experiment planned at GANIL in 2011.

# Comparison with FOPI

$$vartl = \frac{\text{var}(y_{\perp})}{\text{var}(y_{\parallel})}$$



# Comparison IQMD<sup>1</sup>



<sup>1</sup>J.-Y. Liu, *et al.*, PRL **86** 975 (2001)



Imbalance ratio  ${}^3\text{He}/t$ 